Recent Developments in Waves Simulation JOSO 2025

SYLVAND Guillaume & 1XRV / CONCACE team @ Airbus Central R&T 18 March 2025



Outline

- Industrial Context
- Waves Applications
- Overview of current works
 From formulations...
 ... to HPC solvers
- Perspectives & Conclusion

Airbus CRT (Central Research & Technology)

- Cross-divisional R&T organization
- Preparing the company's long-term technological capabilities
- ~160 people (60% PhDs)
- Located in 3 countries
- 5 domains:



6 CRT sites in Germany, France, UK



Virtual Product & Engineering

- Upstream research in modelling and simulation for our products, systems and operations.
- ~40 peoples
- Human Focused Technology
- Systems Engineering
- Modeling
- Computing for Simulation
- Applied Mathematics for Modeling & Simulation





Waves Applications @ Airbus

- Electromagnetism: Antenna placement, EMC, RCS
- Acoustics: Noise propagation around aircrafts
- CRT position: not in competition with commercial softwares



Mathematical Formulation

- Problems of similar sizes in both physics
- Integral Equations solved by Boundary Element Method
 - + extra "refinements" when needed
- Advantages: Accuracy, easier to mesh.
- Drawbacks: dense linear system, only homogeneous propagation media.



Existing Methods & Tools

- **BEM** formulation coupled with (volume) **FEM** formulation for heterogeneous parts
- Fast dense solver using Hierarchical Matrices (or FMM, but not in this talk !)
- Using High Performance Computing



Limitations / Difficulties

- Scalability (for H-matrix)
- Modelling of heterogeneous domains
- Modelling/meshing of complex details

Active Researches

Working at different levels:

- Formulation/Modelisation
- Meshing / Data preparation
- Solver / Hybridization of solvers

Quasi-Trefftz Discontinuous Galerkin Method

Learning Based Rank Estimator Learning Approach to Geometry Simplification Upgrading H-matrix solver Composability applied to FEM-BEM Coupling

Quasi-Trefftz Discontinuous Galerkin Method

- Application : wave propagation in partly homogeneous / partly heterogeneous domains (Jet flow, boundary layer)





Quasi-Trefftz Discontinuous Galerkin Method

- Convected Helmholtz Equation
- Today : FEM/BEM Coupling



Quasi-Trefftz Discontinuous Galerkin Method

- Limitations:
 - PDE coefficients constant per element
 - Fine mesh (λ /15)
- Solution proposed (PhD of Andrea Lagardère)
 - Use Quasi-Trefftz functions in DGM coupled with BEM

Several kinds of quasi-Trefftz functions		
• Amplitude based :	$P(oldsymbol{X})e^{ioldsymbol{k}_{0}\cdotoldsymbol{X}}$,	$ oldsymbol{k}_0 ^2=\kappa^2(oldsymbol{x}_0)$,
• Phase based :	$e^{Q(oldsymbol{X})}$,	$Q(oldsymbol{X}) = ioldsymbol{k}_0\cdotoldsymbol{X} + H.O.T.$,
• Polynomial functions :	$R(oldsymbol{X}).$	

Quasi-Trefftz Discontinuous Galerkin Method

- Work in Progress (finishing 1st year of PhD)
- Pre-existing:
 - Airbus FEM-BEM code & application
 - L.M. Imbert-Gérard QT construction methodology
 - Makutu extensive knowledge of DGM
- Done:
 - Build QT function for heterogeneous Helmholtz (without convection) + mockup 2D
 - Theoretical work for convected Helmholtz in DGM
- Next:
 - Mockup for convected Helmholtz in 2D, 3D
 - Full testing (accuracy ? size of elements ? performance vs. FEM ?)
 - Coupling with BEM
 - Industrial Applications
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Upgrading H-matrix solver

- CIFRE PhD "Composabilité en Algèbre Linéaire Haute Performance Application à l'Aéroacoustique et à l'Électromagnétisme" started january 2025 by Clément Peaucelle (@Airbus, Issy)
- Push further the H-matrix approach
- Reminder : H-matrix is a hierarchical approximate low-rank matrix format, very efficient on dense matrices coming from IE+BEM





$$A \approx \begin{bmatrix} r & m \\ x & V & r \\ n \\ r = rank \text{ of } A(n, m) \end{bmatrix}$$

 $Memory \ footprint = \ rank * (n + m)$

Approximate Low-Rank Block

Upgrading H-matrix solver

- Implemented with task-based programming on top of StarPU
- Factorisation in $\mathcal{Q}(n^{\alpha} \log n)$ instead of $\mathcal{Q}(n^{3})$
- But...
 - Poor scalability
 - High memory consumption





Upgrading H-matrix solver

Directions investigated:

- Floating point lossy compression (e.g. <u>https://szcompressor.org/</u>)
 Ignore digits that are "beyond" the accuracy of our low-rank compression
 Potential to have memory reduction by a factor 3 or 4
 (in progress : see you at COMPAS 2025 <u>https://2025.compas-conference.fr/</u>)
 Next:
 - Enhance scalability by splitting large low-rank blocks not in the *rows* or *columns* dimension, but in the *rank* dimension Side effect: allow larger blocks, hence memory reduction
 - Use of GPU for some tasks
 - Use of Randomized Algorithms
 - etc.

Learning Based Rank Estimator

- In H-matrix solver: rank estimator needed
 - Does a low-rank block fit in memory ?
 - Should we keep it or subdivide it ?
- Today: basic estimator
- Let's use learning-based methods !



Learning Based Rank Estimator

- Objective: Given a block of matrix (set of row & columns unknowns), estimate the rank of the blocks with a cheap computation
- PhD of Théo Briquet (@Cerfacs, Toulouse)
- Features:
 - We don't have : the block content, the actual rank
 - We do have : geometry (bounding boxes, diameters, distance, visibility factor), physics involved (Maxwell, Helmholtz, Laplace, etc.), physical parameters (λ, ε, μ)
- Learning using random forests



Learning Based Rank Estimator

- Each decision tree is built on a (random) subset of the data
- 2 separate studies (regression or classification)
 - Estimate the rank or
 - Estimate if the block fits in memory



- Next steps
 - Try other ML techniques
 - Connect to Applications
 - Industrial test-cases
 - More physics
 - etc.





Composability applied to FEM-BEM Coupling

- Same application as QT DGM: Aeroacoustics... ...but on the purely algebraic solver side
- Mixed Matrix with
 - BEM in homogeneous domain s ~10⁶ unknowns
 - FEM in heterogeneous domain v ~10⁹ unknowns

Too dense for sparse solvers, too large for dense solvers... ... need to develop new approaches







Composability applied to FEM-BEM Coupling

- In the past: coupling existing sparse & dense solvers (H-Matrix + MUMPS) -A lot of algorithms : multi-solve, multi-facto Limited by the solvers interfaces Perspective 1 - possibilities
- Post doc of **Esragül Korkmaz** (@Inria, Bordeaux)

Ideas :

- Handle all the system with 1 H-matrix
- Use two task-based solvers (QR-MUMPS & H-mat) -
- Compare all these possible approaches
- Industrial applications
- etc.

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Direct Solver Iterative Solver • Coupled with schur Coupled Multifacto • (Mumps, Hmat) • (Mumps, Spido) • (qr_mumps, Hmat) • (*qr_mumps*, Spido) Multisolve • (Mumps, Hmat) • (Mumps, Spido) • Coupled with schur • (*qr_mumps*, *Hmat*) • (*qr_mumps*, Spido) • 1 stage

- (*qr_mumps*, *Hmat*)
- Not coupled (1 big matrix)
- Hmat

- With preconditioner (e.g. Mumps, Spai, Hmat)
 - Diff dense matrix formats: Spido, FMM, Hmat
- Without preconditioner
 - Diff dense matrix formats: Spido, FMM, Hmat
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Learning Approach to Geometry Simplification

Some details on the structures (slots, wires, etc.) have to be finely handled →expansive data preparation & computation

Idea: use learning approach to find Equivalent Models

Post-doc of **Augustin Leclerc** (@Airbus, Issy)



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Also in progress: PINN (PhD of Joel SOFFO)



Jobs available

- Apprenticeship in Issy (Paris area) on HPC/GPU Search "HPC" on <u>airbus.com/en/careers</u>
- Post-doc in Inria Bordeaux on Numerical Linear Algebra / Low Rank Algorithms <u>https://recrutement.inria.fr/public/classic/fr/offres/2025-08695</u>

Thank you

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